



# **Nobelio fizikos 2021 metų premija. Laureatai ir jų tyrimai**

## **Bronius Kaulakys**

**Vilniaus universitetas  
Teorinės fizikos ir astronomijos institutas**

# The Nobel Prize in Physics 2021

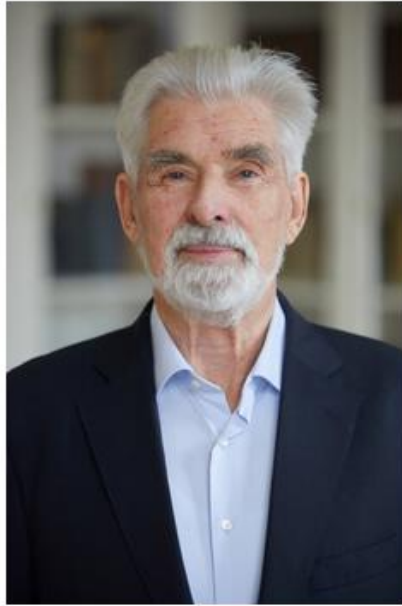


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Risdon Photography

**Syukuro Manabe**

Prize share: 1/4

Gimė 1931 m. Mokėsi Tokijo universitete, Japonija. Dirbo Prinštone universitete, JAV



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Bernhard Ludewig

**Klaus Hasselmann**

Prize share: 1/4

Gimė 1931 m. Mokėsi ir dirbo Hamburgo universitete ir Makso Planko institute, Vokietija



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Stefan Bladh

**Giorgio Parisi**

Prize share: 1/2

Gimė 1948 m. Mokėsi ir dirba Romos Sapienza universitete, Italija. La Sapienza -didžiausias Europoje įkurtas 1303 m. universitetas

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**2021 m. Nobelio fizikos premija už „novatoriškus indėlius didinant mūsų supratimą apie sudėtingas (kompleksines) fizikines sistemas“**

**The Nobel Prize in Physics 2021 was awarded "for groundbreaking contributions to our understanding of complex systems"**

**Pusė premijos už "Žemės klimato fizinį modeliavimą, kintamumo kvantifikaciją ir patikimą pasaulinio atšilimo prognozavimą"**

**with one half jointly to Syukuro Manabe and Klaus Hasselmann "for the physical modelling of Earth's climate, quantifying variability and reliably predicting global warming"**

**Kita premijos pusė už "netvarkos ir fluktuacijų tarpusavio sąryšio fizinėse sistemose, pradedant atomų, baigiant planetų lygmeniu, atradimą"**

**and the other half to Giorgio Parisi "for the discovery of the interplay of disorder and fluctuations in physical systems from atomic to planetary scales."**

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**Prof. S. Manabe**, gimęs 1931 m. Šingu, Japonijoje, dirba Prinstono universitete – meteorologas ir klimatologas – **vienas pirmųjų pastebėjęs, kad anglies dvideginis prisideda prie atmosferos kaitimo ir visuotinio atšilimo.**

Anglies dvideginio koncentracija atmosferoje didina Žemės paviršiaus ir troposferos (iki 10 km virš Žemės) temperatūrą (**Šiltnamio efektas**), bet mažina stratosferos (tarp 10 ir 50 km virš Žemės) temperatūrą. Tai buvo ir yra toliau intensyviai plėtojama.

Meteorologo ir okeanografo **K. Hasselmanno** tyrimai daugiausia susiję su orų prognozėmis ir klimato kaita. **Prof. K. Hasselmannas**, gimęs 1931 m. Hamburge, Veimaro respublikoje, dirba Makso Planko institute Hamburge. Labiausiai žinomas kaip jo vardu pavadinto modelio, **Hasselmann model**, autorius. Šis modelis **susieja ilgus atminties vandenynų raidą su sparčia, sunkiai numatoma orų ir klimato kaita.**

**Prof. G. Parisi**, gimęs 1948 m. Romoje, – labai garsus, plataus masto daug padaręs **fizikas teoretikas**. Dirba Romos „La Sapienza“ universitete.

Jo tyrimų sritys apima **nuo kvantinės chromodinamikos, medžiagų sandarų formavimosi, iki viesulų ir paukščių būrių susidarymo.**

Jis atliko **fundamentalius teorinius darbus statistinės fizikos, kuri plėtojama jau daug dešimtmečių, srityje.**

Žinomos ir plačiai naudojamos **fundamentalios lygtys, kurių pavadinimuose yra prof. G. Parisi pavardė.**

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## Oficialus Nobelio fizikos komiteto premijos skyrimo pagrindimas

Scientific Background on the Nobel Prize in Physics 2021  
“FOR GROUNDBREAKING CONTRIBUTIONS TO OUR  
UNDERSTANDING OF COMPLEX PHYSICAL SYSTEMS”  
The Nobel Committee for Physics

Pradedamas nuo  
Įvado

“This year's Nobel Prize in Physics focuses upon **the complexity of physical systems, from the largest scales experienced by humans, such as Earth's climate, down to the microscopic structure and dynamics of mysterious and yet commonplace materials, such as glass.**”

Toliau nuo nestabilumo, netiesiškumo, daugia-masteliškumo, kompleksiškumo ir stochastiškumo

A. Instability and nonlinearity underlie multiscale complexity and stochasticity

Nuo laminaraus ir turbulentinio judėjimo (**1953** m. monografija), tvarkos ir netvarkos...

**B. B. Mandelbrot** straipsnio ir t. t.

link klasikinio **Edward Lorenz 1963** m. Deterministic nonperiodic flow. J. Atmos. Sci. **20**, 130 ir kitų darbų.

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## Lorenco lygtys

$$\begin{aligned}\frac{dX}{dt} &= \sigma(Y - X), \\ \frac{dY}{dt} &= X(Ra - Z) - Y \quad \text{and} \\ \frac{dZ}{dt} &= XY - \beta Z,\end{aligned}$$

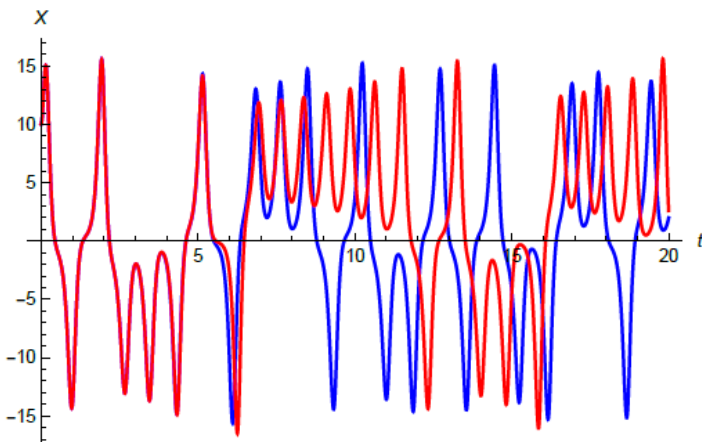


FIG. 2. Plot of  $X(t)$  of the Lorenz system with  $(\sigma, \beta, Ra) = (10, 8/3, 24.9)$  in which the initial data for all three variables are 10 (blue) or 10.01 (red). The divergence of the two solutions with slightly different initial conditions begins at  $t = 5.5$ ; this is sensitive dependence on initial conditions, often whimsically referred to as the “Butterfly Effect”.

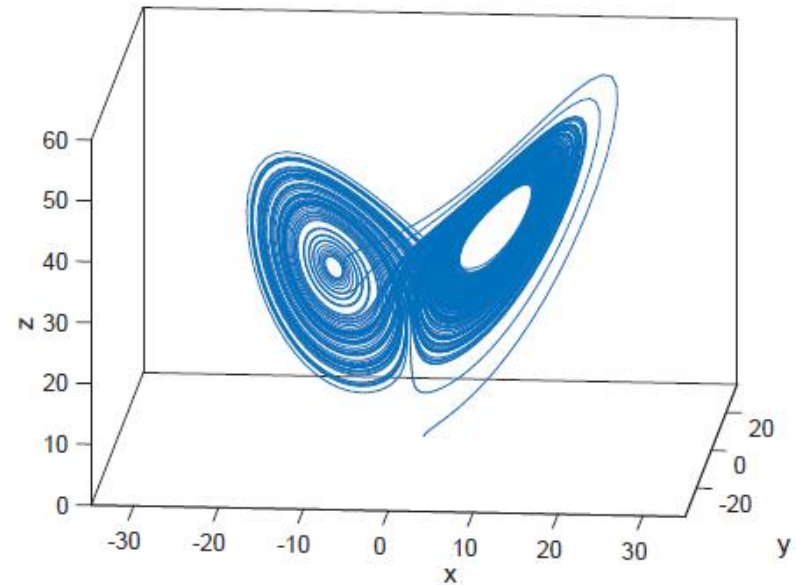


FIG. 1. Plot in  $(X, Y, Z)$  phase space of numerical simulation of a circuit version of Lorenz system at  $(\sigma, \beta, Ra) = (10, 8/3, 33.5)$ , from Weady *et al.* (2018).

Prof. Kęstučio Pyrago dažnai rodomi paveikslai pasakojant apie deterministinį (dinaminį) chaosą



Jo straipsnis, nors nėra tiesiogiai siejamas su Lorenz sistema, bet str. K. Pyragas, *Continuous Control of Chaos by Self-Controlling Feedback*, Phys. Lett. A **170**, 421-427 (1992). **Cituotas apie 3000 kartų.**

Kituose strainsniuose nagrinėjama ir Lorenz sistema:

V. Pyragas, K. Pyragas, *Delayed feedback control of the Lorenz system ...Phys. Rev. E* **73**, 036215 (2006).

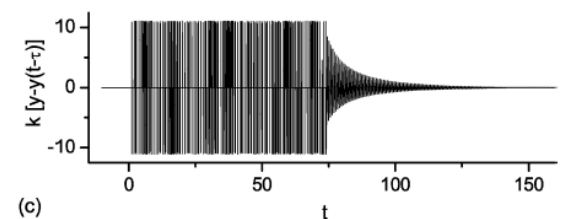
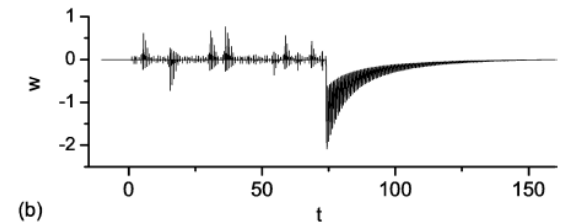
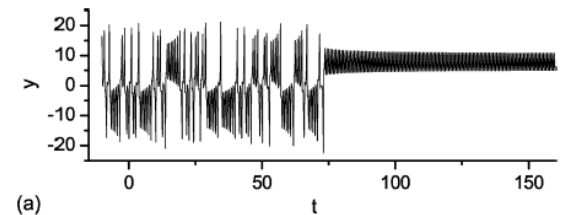
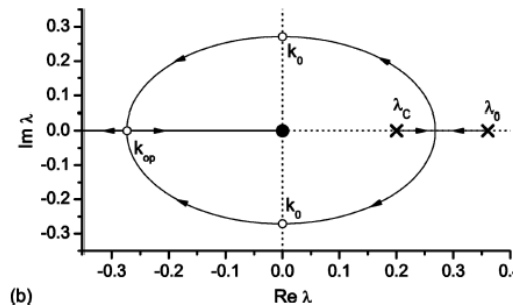
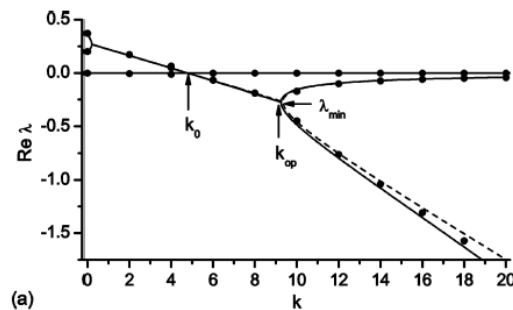
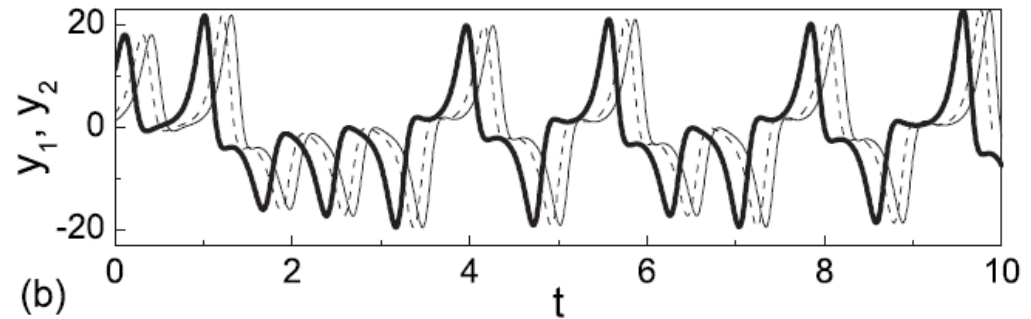
V. Pyragas, K. Pyragas, *Analytical treatment of the delayed feedback controlled Lorenz system close to a subcritical Hopf bifurcation, Lith. J. Phys.* **48**, 5 (2008).

K. Pyragas, T. Pyragienė, *Phys. Rev. E* **78**, 046217–4 (2008).

$$\dot{x} = \sigma(y - x),$$

$$\dot{y} = rx - y - xz,$$

$$\dot{z} = xy - bz,$$





Kitas skyrelis

## B. Stochasticity and Disorder Imply Predictability

Kalbama apie signalo ir triukšmo santykį **klasikiniame Brauno judėjime pusiausvyros atveju**, kai yra tolygusis pasiskirstymas (equipartition).

Ir kai yra **nukrypimas nuo pusiausvyros**.

Tada **situacija yra dramatiškai kitokia**:

Cituojamas **Giorgio Parisi** straipsnis

**year of physics concept**

# Brownian motion

Giorgio Parisi

*“I did not believe that it was possible to study the Brownian motion with such a precision.”  
From a letter from Albert Einstein to Jean Perrin (1909).*

**Mintis** “But the situation is different for systems that are only slightly out of equilibrium. ... this situation typically applies to disordered systems, such as **spin glasses** and **structural glasses**.”

**Iškyla mikroskopinės trumpų trukmių  
ir makroskopinės ilgų trukmių laikų skalės**

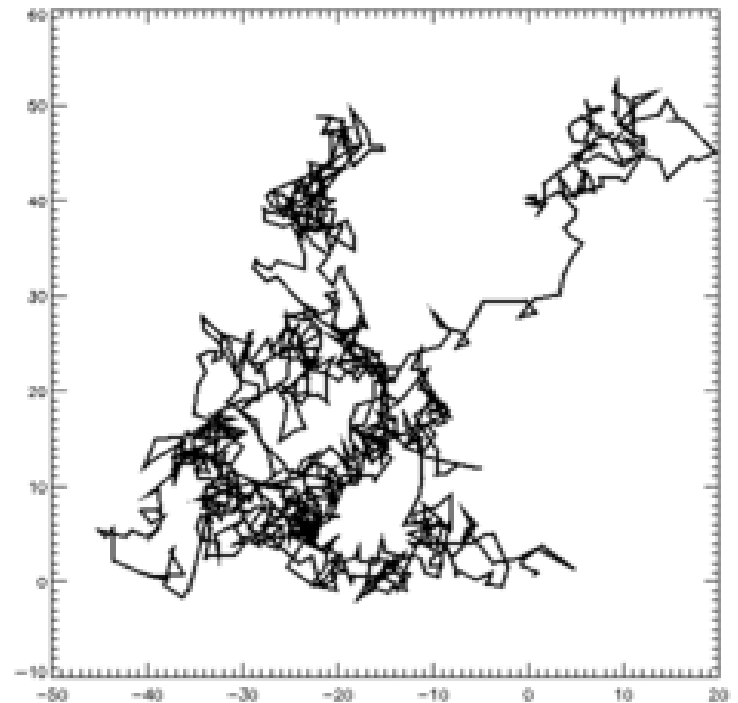


# Brown's molecules (1)

## 1. Robert Brown (1827) "...Microscopical Observation of Active Molecules..."



Brown's molecules  
random walk



# Brown'o judesys (2)

## 2. Louis Bachelier (1900)

“Théorie de la spéculation”

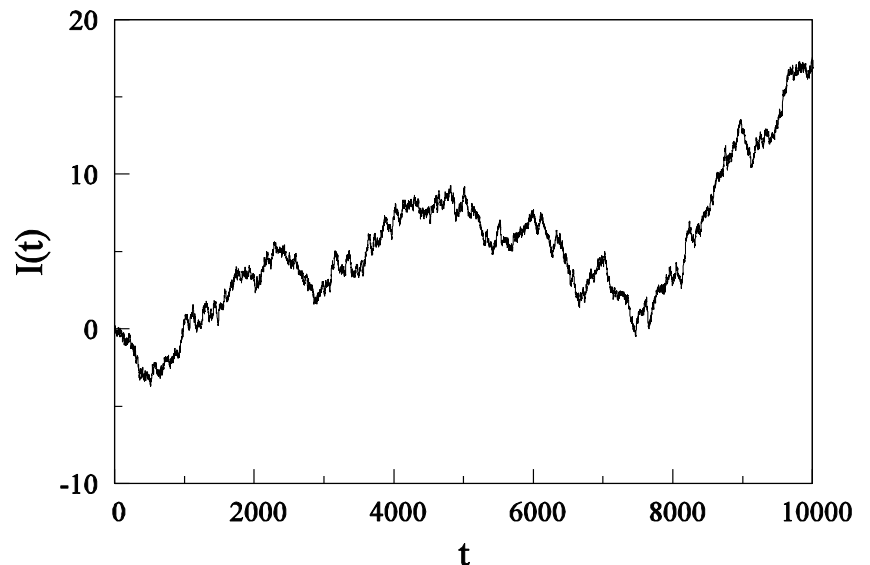
Brown'o judesio teorija

‘Pioneering Econophysics’



Louis  
Bachelier  
(1870-1946)

**Signalo**  
**intensyvumo**  
**Brown'o judesys**



# Brown'o judesys (3)

## 3. Albert Einstein (1905)

*"Über die von der molekularkinetischen Theorie der Wärme geforderte Bewegung von in ruhenden Flüssigkeiten suspendierten Teilchen"*

*("On the Motion—Required by the Molecular Kinetic Theory of Heat—of Small Particles Suspended in a Stationary Liquid")*

## Brown'o judesio teorija

Numatė (patvirtino) molekulinę medžiagos sandarą



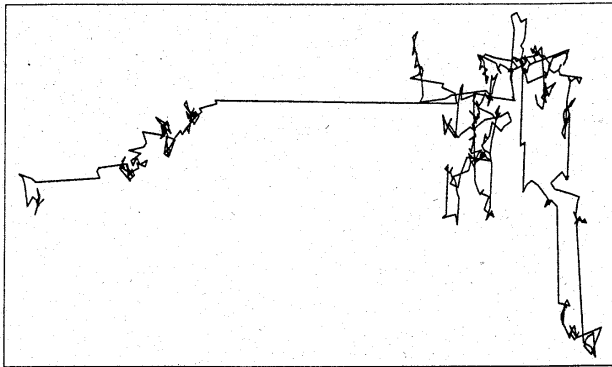
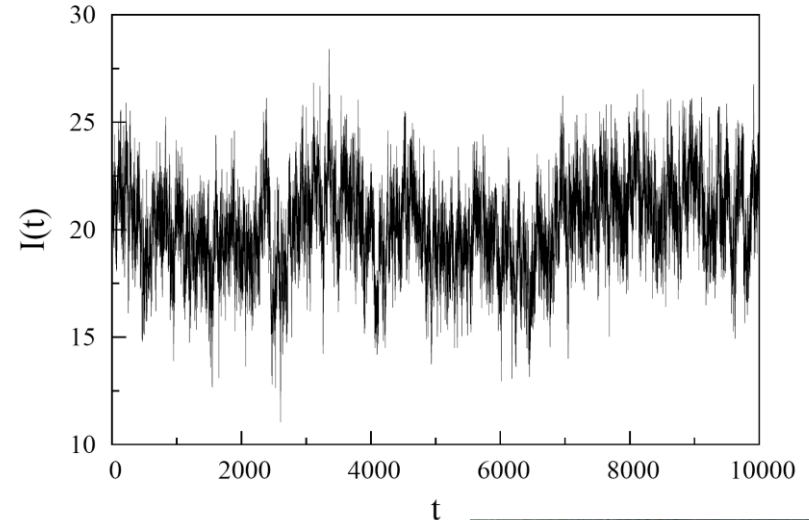
Brown'o judesys erdvėje

# Brown's judesys (4) Matematinė teorija



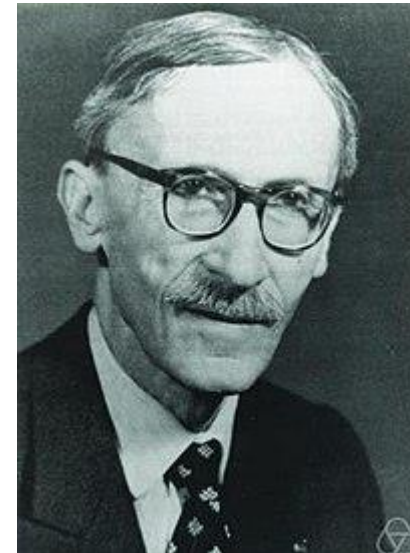
**Norbert Wiener (1923)**  
"continuous-time Gaussian stochastic process with independent increments"

(1909 – 1946)



**Paul Levy (1925, 1937-54)**

"continuous-time stochastic process that has stationary independent increments"  
Lévy flights etc.



**Signalo intensyvumo**

ir/arba

**erdvėje Brown'o judesys**

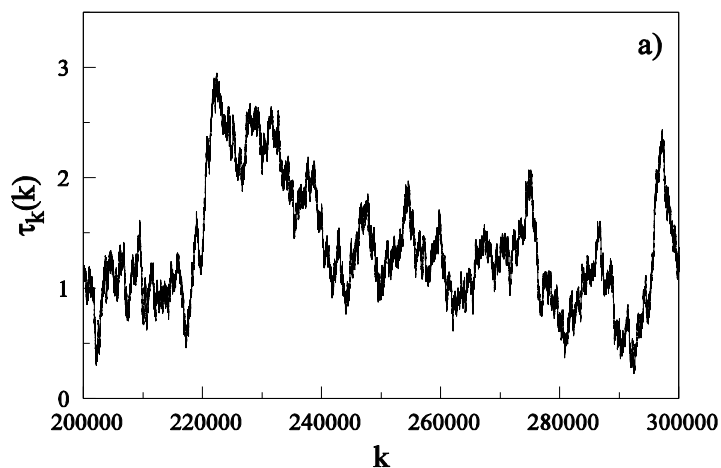
(1886 – 1971)

# Brown'o judesys (5, mūsų)

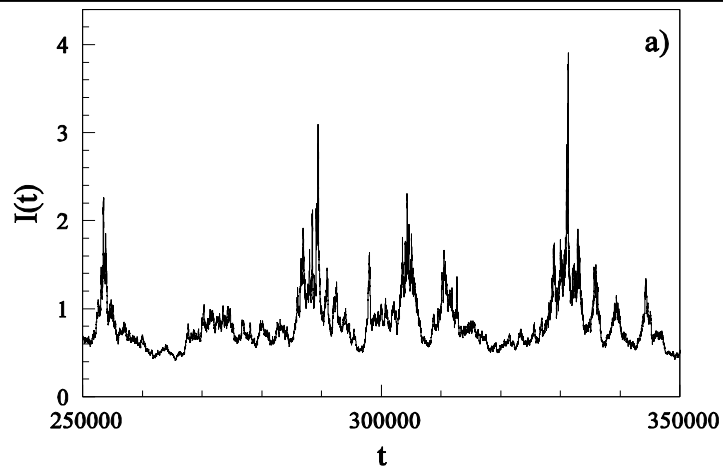
B.Kaulakys, T.Meškauskas, V.Gontis, J.Ruseckas, M.Alaburda  
(1997-2016)

## Brown'o ir Brown'o tipo judesys

**laiko ašyje** (vidutinės trukmės tarp įvykių, impulsų, objektų)  
kaip galimas  $1/f$  fliktuacijų šaltinis



Trukmės tarp įvykių kitimas



Signalas

# Brown'o judesys (6, mūsų)

## Nechaotinis Brauno pobūdžio judėjimas

Dalelių ansamblio atsitiktinis trikdymas gali sinchronizuoti dalelių judėjimą ir sukelti fazinio virsmo analogą – chaotinio judėjimo virsmą nechaotiniu atsitiktiniu judėjimu.

Šie tyrimai sukėlė VU matematikų prof. F.Ivanausko, prof. V.Mackevičiaus ir kt. susidomėjimą

- ✓ B. Kaulakys, G. Vektaris, *Phys. Rev. E* **52**, 2091 (1995).
- ✓ B. Kaulakys, *Nonlinear Analysis: Model. Contr.* **2**, p.43-58 (1998).
- ✓ B. Kaulakys, F. Ivanauskas, T. Meškauskas, *Intern. J. Bifurc. Chaos* **9**, 533 (1999).
- ✓ A. Ambrazevičius, F. Ivanauskas, V. Mackevičius, *Nonlin. Analysis* **93**, 122 (2013).



Consider a system of particles of mass  $m$  moving with friction according to Newton's equations

$$\frac{d\mathbf{r}}{dt} = \mathbf{v}, \quad \frac{d\mathbf{v}}{dt} = -\frac{1}{m} \frac{dV(\mathbf{r}, t)}{d\mathbf{r}} - \gamma \mathbf{v} \quad (1)$$

in the time dependent potential  $V(\mathbf{r}, t)$ , e.g. in the potential  $V(x, t) = x^4 - x^2 - ax \sin \omega t$ , and with the friction coefficient  $\gamma$ .  $\mathbf{v}_k^{\text{ran}}$ :  $\mathbf{v}^{\text{new}} = \alpha \mathbf{v}^{\text{old}} + \mathbf{v}_k^{\text{ran}}$

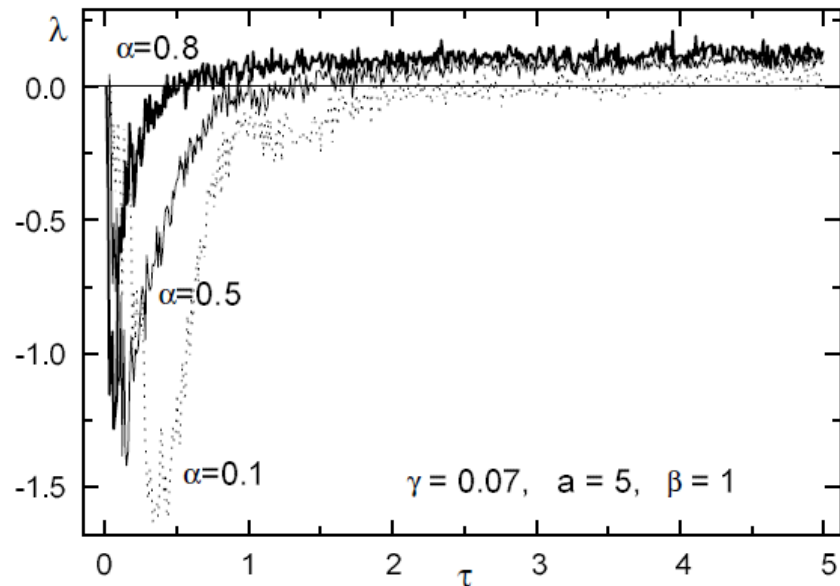


Fig. 7. Lyapunov exponent  $\lambda$  versus the time  $\tau$  between the resets of the velocity  $v^{\text{new}}(k\tau) = \alpha v^{\text{old}}(k\tau) + \beta v_k^{\text{ran}}$ ,  $k = 1, 2, \dots$  for different values of the parameter  $\alpha$  for motion in the driven Duffing potential with friction according to Eq. (8).

Lyapunov exponents or  $KS$  entropy of the system

$$\begin{aligned} \sigma_k &= \left\langle \frac{1}{\tau_k} \ln |\mu_k| \right\rangle \\ &= \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{k=1}^N \frac{1}{\tau_k} \ln |\mu_k(\mathbf{r}_k, \mathbf{v}_k, \tau_k)| \end{aligned} \quad (6)$$

A criterion for transition to chaotic behavior is

$$\sigma_{\text{max}} = 0. \quad (7)$$

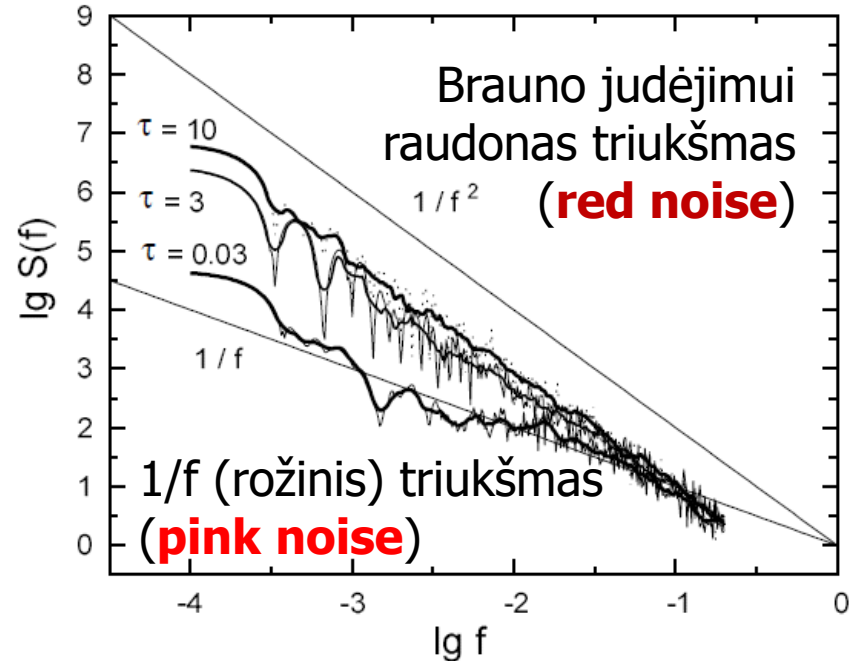


Fig. 8. The power spectral density of the current of the ensemble of particles moving according to Eq. (9) with  $F = 1$ ,  $\gamma = 0.1$  and perturbed by the common for all particles noise



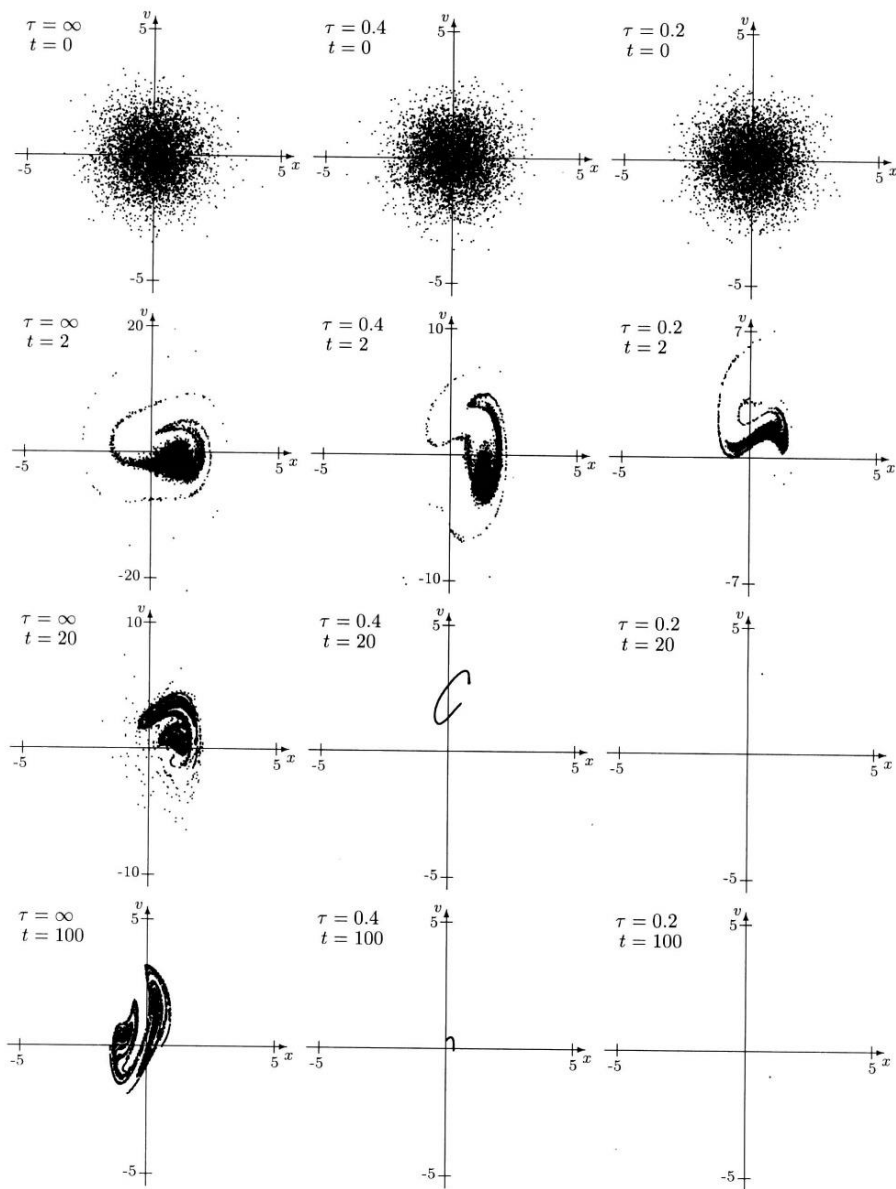


Fig. 6. As in the Fig. 1 but for motion according to Eq. (8) in the nonautonomous Duffing potential with  $\gamma = 0.07$ ,  $a = 5$ ,  $\alpha = 0.8$  and  $\beta = 1$ . A transition from the actual chaotic (at  $\tau = \infty$ ) to the nonchaotic dynamics with the decrease of the time interval  $\tau$  between the resets of the velocity is observable.

## Matematikai išanalizavo griežtai, su lemomis ir teoremomis

A. Ambrazevičius et al. / *Nonlinear Analysis* 93 (2013) 122–131

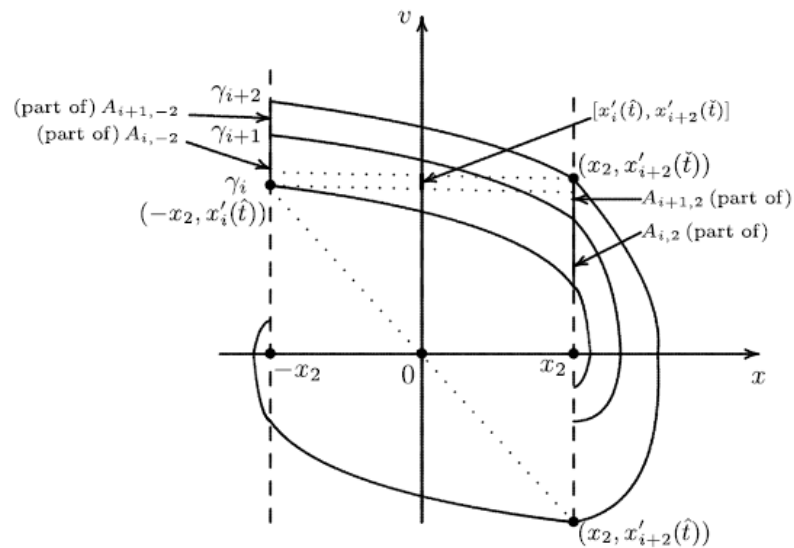


Fig. 2. Illustration to the proof of Lemma 1 ( $m = 2$ ).

## II. CLIMATE PHYSICS: BACKGROUND AND HISTORY

Since **Fourier's** studies of the **Earth's energy budget**....

“**Two hundred years ago, French physicist Joseph Fourier (1768- 1830)** studied the energy balance between the sun’s radiation towards the ground and the radiation from the ground.”

“The heating effect of the absorption of solar radiation by CO<sub>2</sub> and other gases was measured by **Eunice Foote (JAV, 1819- 1888)**, **pirmoji mokslininkė, padariusi išvadą, kad kai kurios dujos įšyla veikiamos saulės spindulių, o didėjantis anglies dvideginio lygis pakeis atmosferos temperatūrą ir gali turėti įtakos klimatui – reiškinyms dabar labai aktualus** but in **1861 John Tyndall** published a then technological tour-de-force of systematic absorption and emission of infrared radiation by a wide variety of gases, including water vapor and CO<sub>2</sub>”,

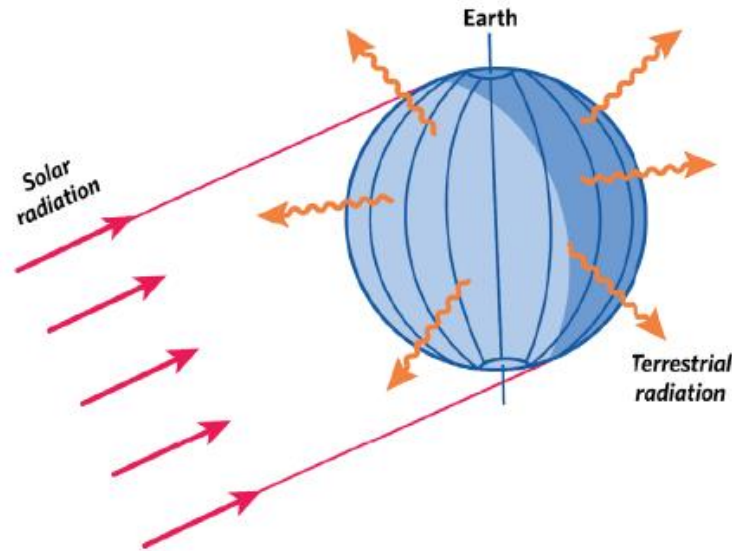
**J. Tyndall**, On the absorption and radiation of heat by gases and vapours, and on the physical connexion of radiation, absorption, and conduction. Philosophical Magazine Series 4 **22**,169-194; 273-285 (**1861**).

.....  
**In the 1950s**, Japanese atmospheric physicist **Syukuro Manabe** was one of the young and talented researchers in Tokyo who left Japan ... and continued their careers in the US. The aim of Manabe’s research, like that of Arrhenius around seventy years earlier, **was to understand how increased levels of carbon dioxide can cause increased temperatures.**

**Syukuro Manabe, Nobel Lecture: Physical modeling of Earth's climate,**  
Rev. Mod. Phys. **95**, 010501 (2023).

“Today, I would like to discuss the role of greenhouse gas in climate change, using relatively simple climate models that we constructed prior to 1990. I begin with the explanation of the so-called **greenhouse effect** of the atmosphere.”

“Radiative transfer from Earth's surface and in the atmosphere obeys Kirckhoff's law.”



$$\text{Outgoing Longwave Radiation} = \sigma \cdot (T_E)^4$$

$$T_E = 255\text{K} \sim -18.7\text{C}$$

$$T_S = 270\text{K} \sim +14.7\text{C}$$

$$T_E - T_S = +33.4\text{C}$$

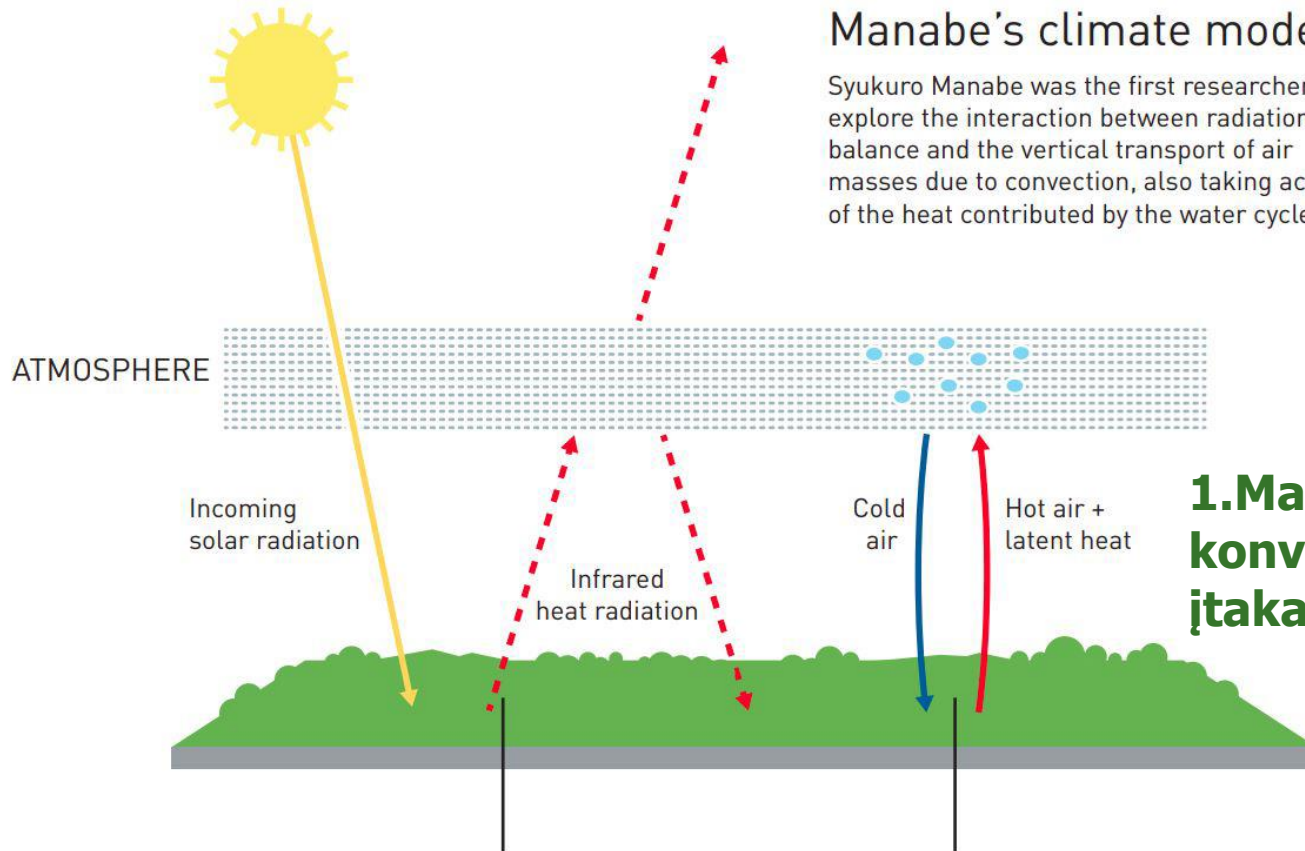
FIG. 4. The temperature thus obtained is  $-18.7^\circ\text{C}$ , which is colder than  $+14.7^\circ\text{C}$ , which is the global mean temperature of Earth's surface. This implies that Earth's surface is warmer than it would be in the absence of the atmosphere by as much as  $33^\circ\text{C}$ . In other words, the atmosphere has a so-called greenhouse effect that increases the temperature of Earth's surface by as much as  $33^\circ\text{C}$ . It is the satellite observation of outgoing longwave radiation that has provided the most convincing evidence for the existence of the greenhouse effect of the atmosphere.

**Be atmosferos Žemės temperatūra  
būtų  $-18,7\text{ C}$ , o yra  $+14,7\text{ C}$ .**

**Skirtumas  $33$  laipsniai !**

## Manabe's climate model

Syukuro Manabe was the first researcher to explore the interaction between radiation balance and the vertical transport of air masses due to convection, also taking account of the heat contributed by the water cycle.



### 1. Manabe – konvekcijas ģitaka

Infrared heat radiation from the ground is partially absorbed in the atmosphere, warming the air and the ground, while some radiates out into space.

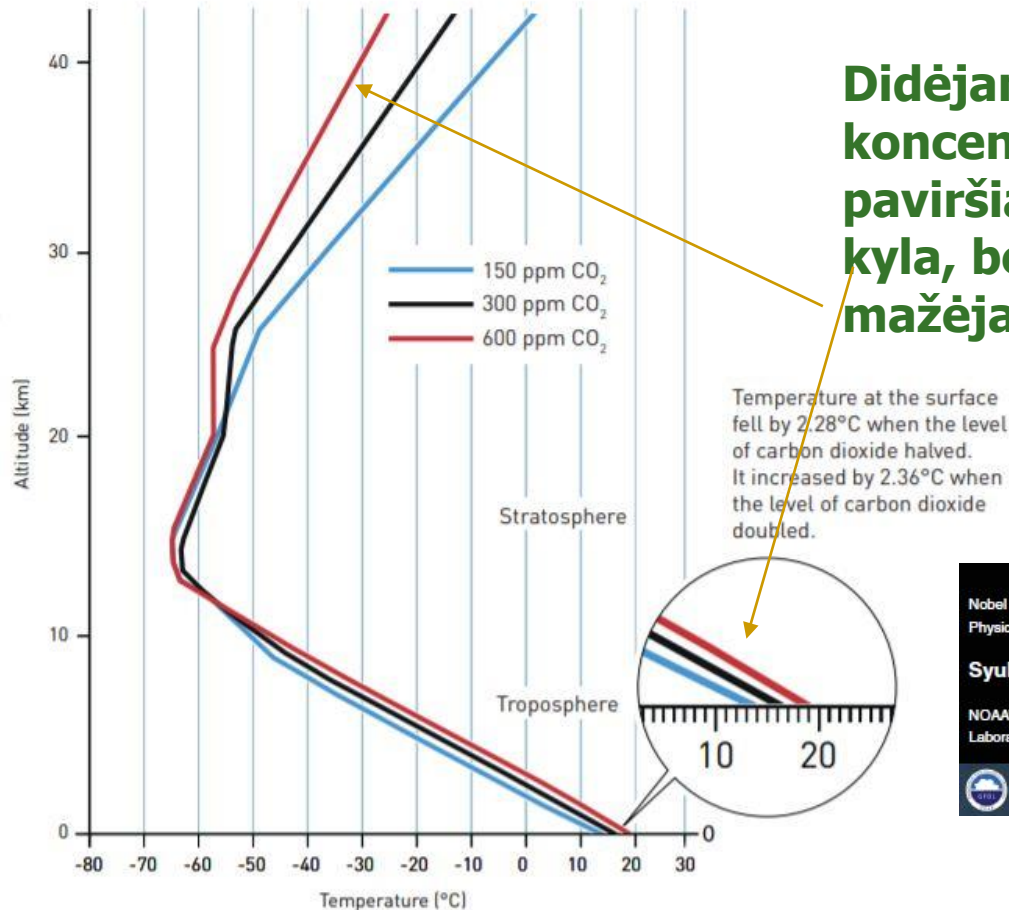
Hot air is lighter than cold air, so it rises through convection. It also carries water vapour, which is a powerful greenhouse gas. The warmer the air, the higher the concentration of water vapour. Further up, where the atmosphere is colder, cloud drops form, releasing the latent heat stored in the water vapour.

### 2. Manabe – vandens garavimo padidējimas ir garu ģitaka šiltnamio efektui

**3. S. Manabe** vienas pirmųjų pastebėjo, kad **anglies dvideginis** prisideda prie atmosferos kaitimo ir visuotinio atšilimo. Anglies dvideginio koncentracija atmosferoje didina Žemės paviršiaus ir troposferos (iki 10 km virš Žemės) temperatūrą (**Šiltnamio efektas**), bet mažina stratosferos (tarp 10 ir 50 km virš Žemės) temperatūrą...

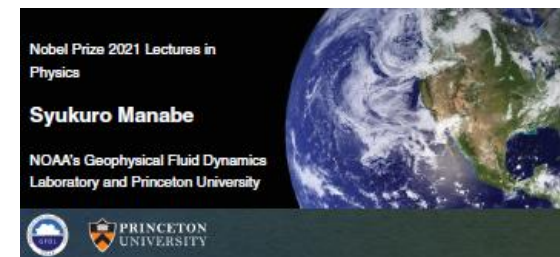
## Carbon dioxide heats the atmosphere

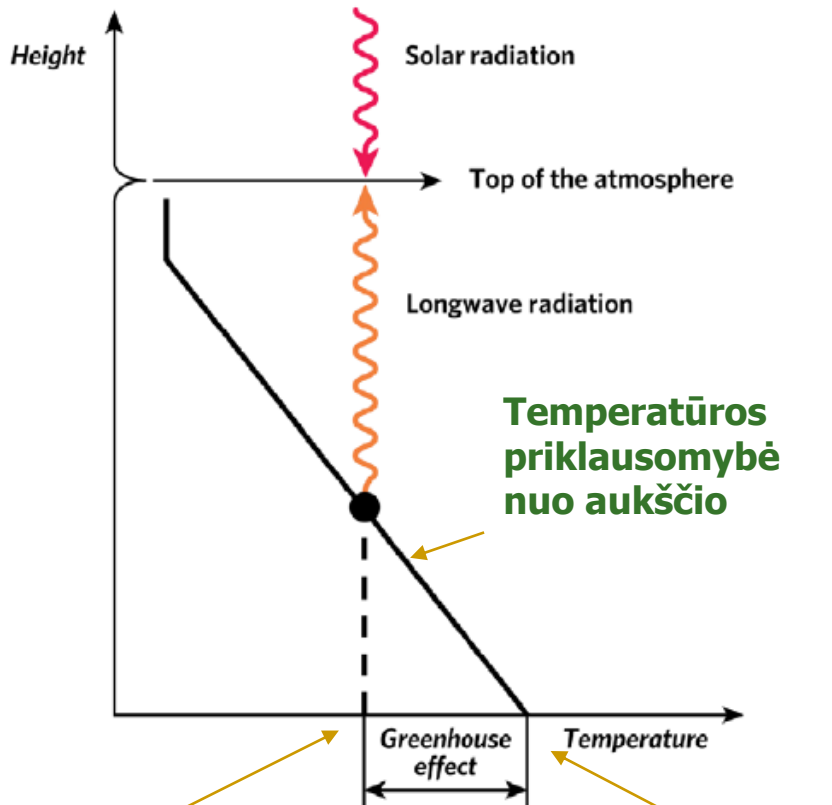
Increased levels of carbon dioxide lead to higher temperatures in the lower atmosphere, while the upper atmosphere gets colder. Manabe thus confirmed that the variation in temperature is due to increased levels of carbon dioxide; if it was caused by increased solar radiation, the entire atmosphere should have warmed up.



**Didėjant CO<sub>2</sub> koncentracijai – Žemės paviršiaus temperatūra kyla, bet stratosferos – mažėja.**

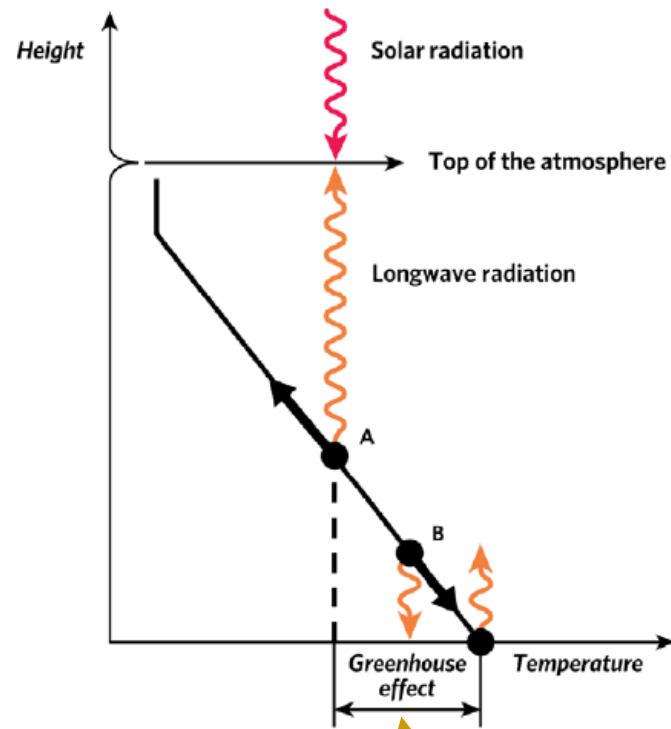
Temperature at the surface fell by 2.28°C when the level of carbon dioxide halved. It increased by 2.36°C when the level of carbon dioxide doubled.





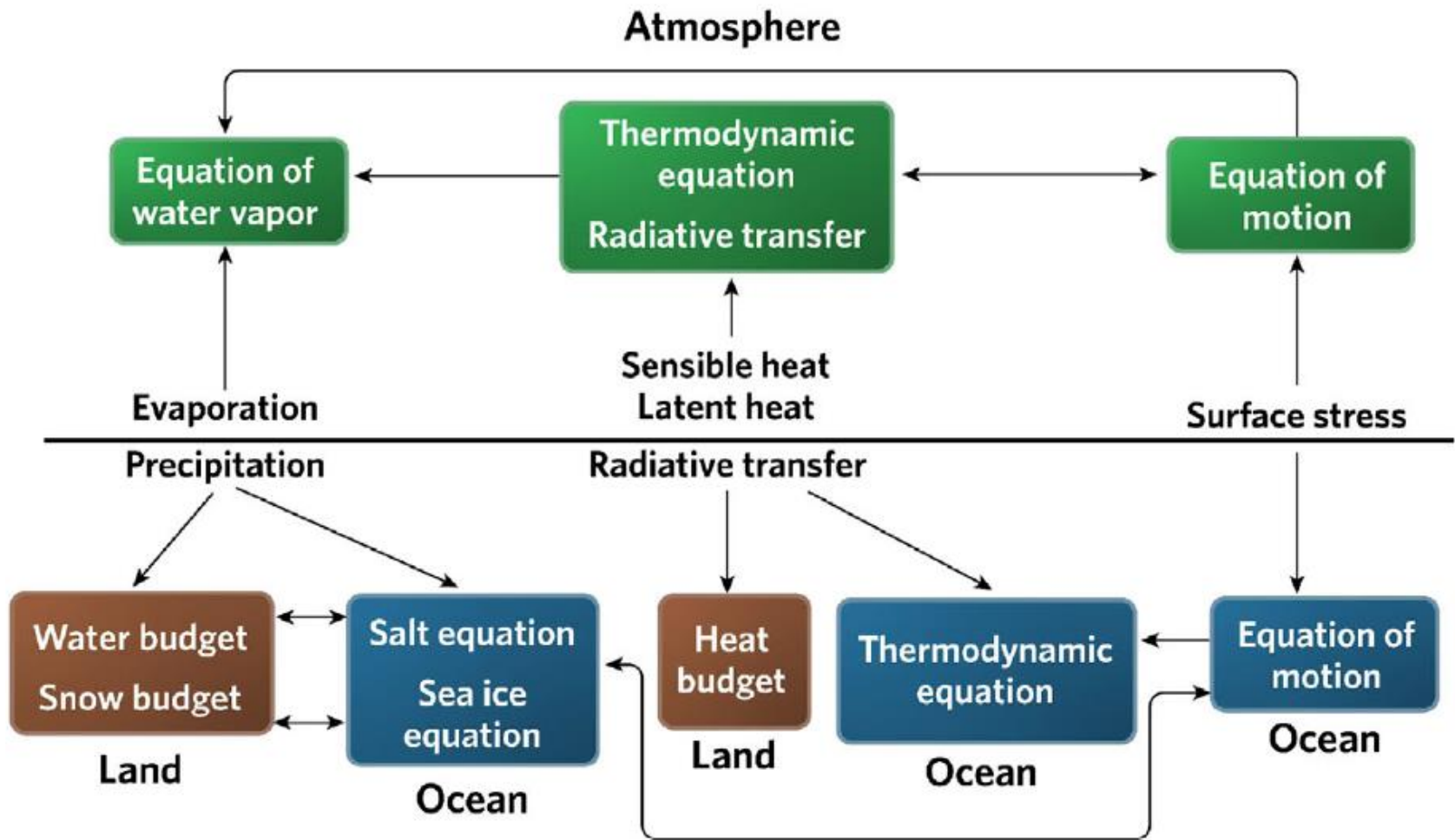
Būtų  $-18,7\text{ C}$   
be dujų šiltnamio  
efekto

Yra  $+14,7\text{ C}$



Kai mažiau skaidri  
atmosfera  
šiltnamio  
efektas stiprėja





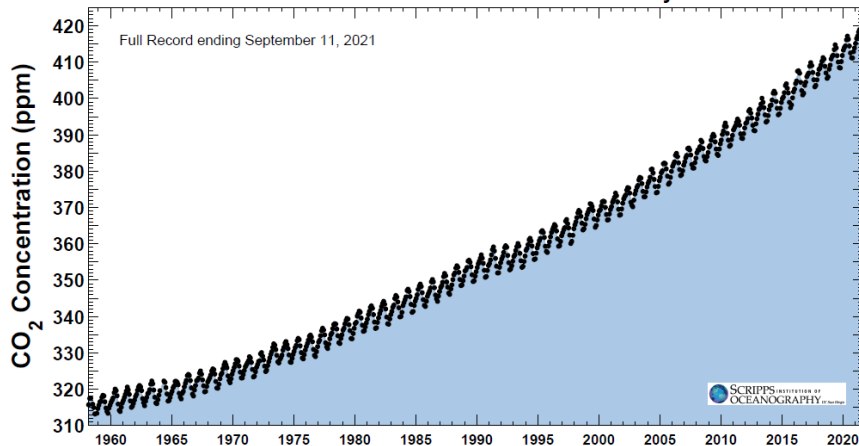
**Pilnesnis šilumos srautų balansas pagal Syukuro Manabe, 1959 and Kirk Bryan 1961, "Climate Calculations with a Combined Ocean-Atmosphere model" (1969).**



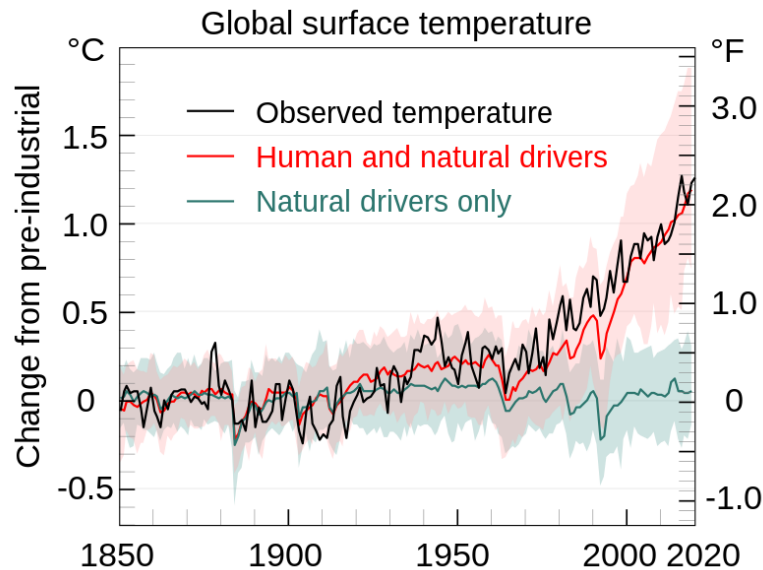
# Anglies dvideginio koncentracija tikrai didėja...

September 10, 2021

Carbon dioxide concentration at Mauna Loa Observatory



## Temperatūra tikrai kyla



## Annual CO<sub>2</sub> emissions

Carbon dioxide (CO<sub>2</sub>) emissions from fossil fuels and industry. Land use change is not included.

Our World in Data

LINEAR

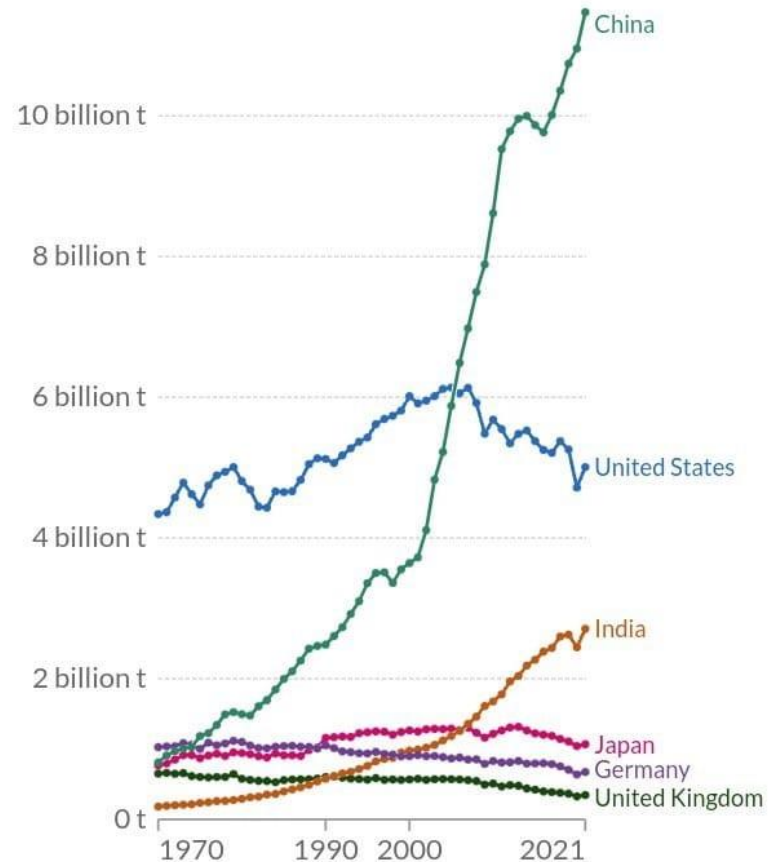
LOG



Add country or region



More



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## Oras yra chaotinis / Weather is chaotic

About ten years **after Manabe, Klaus Hasselmann** succeeded in **linking together weather and climate** by finding a way to outsmart the **rapid and chaotic weather changes that were so troublesome for calculations.**

### Climate Calculations with a Combined Ocean-Atmosphere model

“The **Lorenz system** acts as a rich toy model of **low-dimensional chaos.**”

“**Poincare (Anri Puankarė, 1854-1912, prancūzų matematikas, fizikas, filosofas. Laikomas paskutiniu matematiku – universalu, suvokusiu visas matematikos šakas)** is generally credited with launching the field by **discovering that the long-term behavior of the three-body problem was infinitely more complex than had been anticipated.**”

“He recognized that the solar system could be viewed dynamically as a perturbation of the integrable **Kepler (Hamiltonian)** problem.”

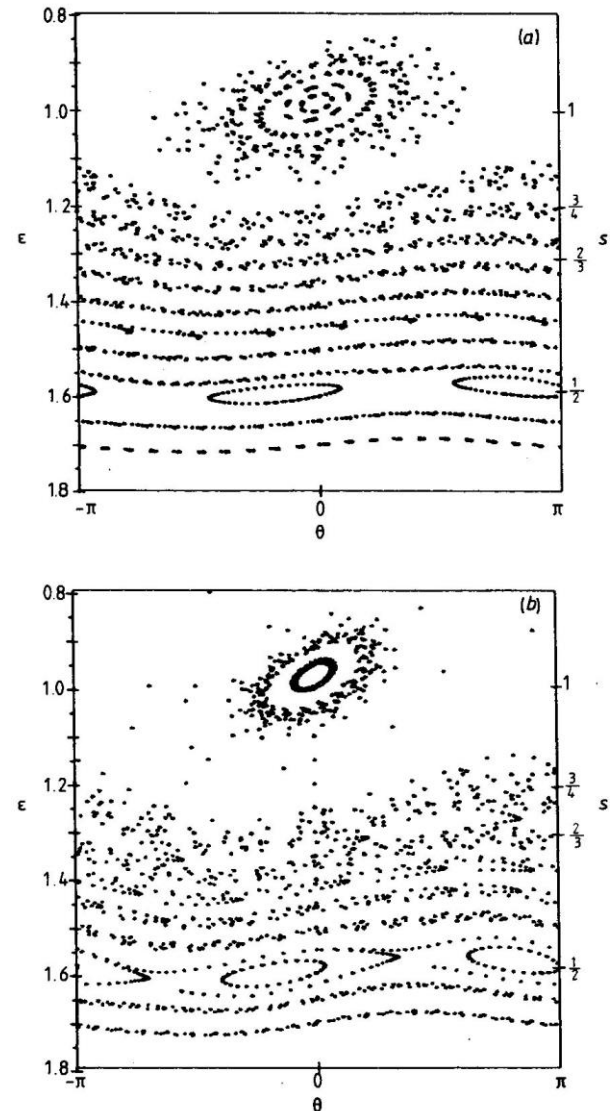
**Mažų dimensijų sistemų chaosą nagrinėjome ir mes jau labai seniai ir gavome “Keplerio atvaizdą”**

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# Tirti netiesinių klasikinių ir kvantinių sistemų chaotinės dinamikos ypatumai, pvz., atomų chaotinė (difuzinio tipo) jonizacija vienspalviame, daugiaspalviame bei impulsiniame elektromagnetiniuose laukuose.

## Gauti rekurentiniai sąryšiai (“Keplerio atvaizdas”)

- ✓ V. Gontis, B. Kaulakys, J. Phys. B: At. Mol. Phys. 20, 5051 (1987).
- ✓ B. Kaulakys, D. Grauzhinis, G. Vilutis, Europhys. Lett. 43, 123 (1998).
- ✓ B. Kaulakys, G. Vilutis, **Kepler map**, Physica Scripta 59, p. 251-256 (1999).
- ✓ M. Alaburda, V. Gontis, B. Kaulakys, Lith. J. Phys. 40, 242 (2000).



**Figure 2.** Trajectories for the map (14) with equations (18) and (19) on the plane  $(\theta, \epsilon)$ . (a)  $\pi\epsilon_0^2\Phi_0 = 0.06$ ; (b)  $\pi\epsilon_0^2\Phi_0 = 0.12$ . The initial conditions are  $\theta_0 = 0$ ,  $\epsilon_0 = \epsilon_i$  ( $i = 0, 1, 2, \dots$ ).

## Klause Hasselmanno darbai

with a **long memory** (the ocean) He is best known for developing the *Hasselmann model* of **climate variability** ... system integrates stochastic forcing, thereby **transforming a white-noise signal** into a **red (Brownian) noise** ... **swell waves**). "Analysis of observations of the spectral properties of pressure fields ... motivated Mitchell to posit an autonomous **Langevin equation** description of the ocean climate. .... **Klaus Hasselmann** was creatively using **fundamental physics concepts** to quantify the surface ocean wave **spectra** [1, 2], ... the nature of **fluctuations** ... and **Lorenz's chaotic weather** ... he derived a generalizable **stochastic description** of ocean climate in which the "noise" is associated with the "weather"... [3, 4].

... provided both the motivation and the observational structure for climate scientists to address **variability**.

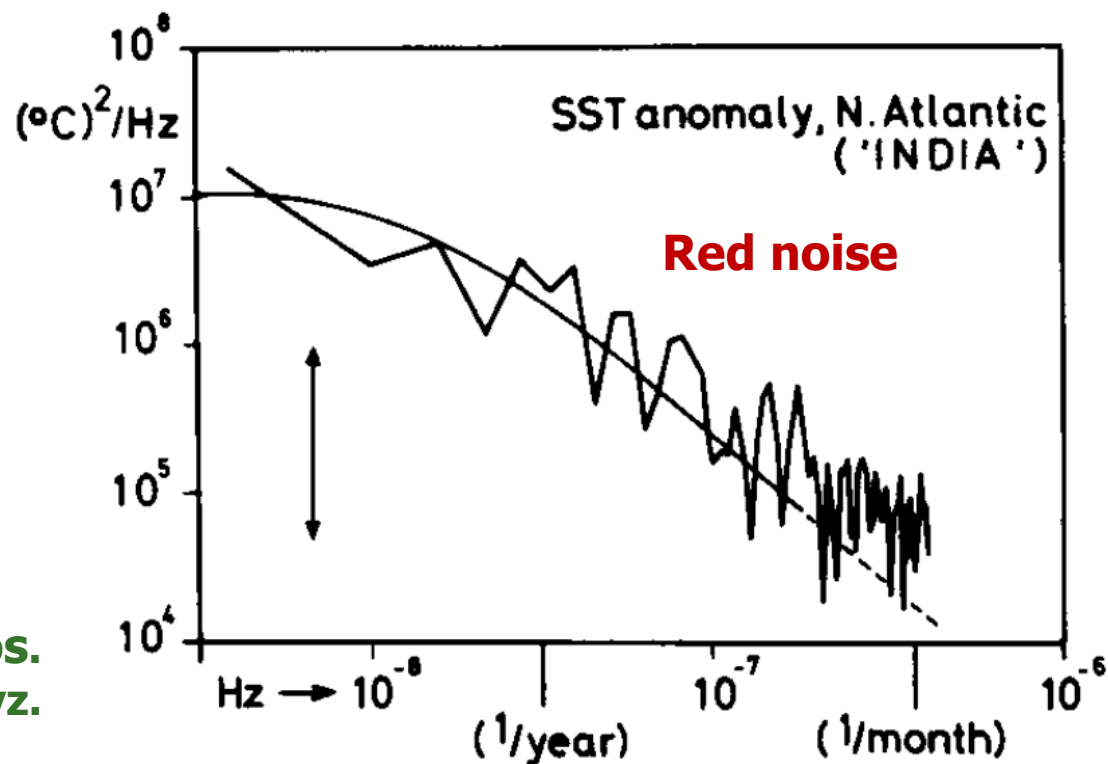
1. **K. Hasselmann**, **Feynman diagrams** and interaction rules of wave-wave scattering processes. Rev. Geophys. **4**, 1 (**1966**).
2. **K. Hasselmann**, **Non-linear interactions** treated by the methods of **theoretical physics** (with application to the generation of waves by wind). Proc. R. Soc. A **299**, 77 (**1967**).
3. **K. Hasselmann**, **Stochastic climate models**, part I. Theory, Tellus **28**, 473 (**1976**).
4. C. Frankignoul, **K. Hasselmann**, **Stochastic climate models**, Part II. Application to sea-surface temperature anomalies and thermocline variability. Tellus 29, 289305 (**1977**).
5. **K. Hasselmann**, 1997. Multi-Pattern Fingerprint Method for Detection and Attribution of Climate Change. Clim. Dyn. **13**, 601 (**1997**).

The first application of the **Hasselmann stochastic model** [3] for climate variability to climate data [4]. **The spectrum** of the Sea Surface Temperature (SST) in the period 1949-1964 in the North Atlantic.

**Stebimos ir 1/f fluktuacijos.**  
**Cituojami ir mūsų darbai, pvz.**  
**Straipsniuose:**

"1/f model for long-time memory of the **ocean surface temperature**, Phys.Rev E (2004);

... "vertical high-resolution distributed-temperature-sensing system"..  
HYDROLOGY AND EARTH SYSTEM SCIENCES (2011)



"**Tropical convective variability as 1/f noise**", JOURNAL OF CLIMATE (2001)

"Thermal convection..." PHYSICAL REVIEW FLUIDS (2020)

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**Orai, klimatas, milžinišką įtaką jiems turintys vandenynai yra labai sudėtinga sistema**, ją modeliuojant atliekami sudėtingi skaičiavimai. Prognozuojant klimato šilimą dirba didžiulės tarptautinės mokslininkų grupės, o

**Manabe ir Hasselmannas tokiems tyrimams padėjo pamatus.** Nobelio premija šiems mokslininkams skirta dar ir todėl, kad **globalinio atšilimo problema yra labai aktuali.**

### **Keletas solidžiausių straipsnių:**

Y. Pomeau, The long and winding road.. **Nature Phys.** **12**, 198 (2016).

K. Hamilton, At the dawn of global climate modeling: the strange case of the Leith atmosphere model, Hist. Geo Space Sci. **11**, 93 (**2020**).

M. Ghil, V. Lucarini, The Physics of Climate Variability and Climate Change. **Rev. Mod. Phys.** **92**, 035002 (**2020**).

M.E. Mann, B.A. Steinman and S.K. Miller, Absence of internal multidecadal and interdecadal oscillations in climate model simulations. **Nat Commun** **11**, 1 (**2020**).

**Spalio 24 d. minima klimato kaitos diena.** Šylant klimatui, kyla pavojus gyvybės Žemėje išlikimui. Klimato kaitą sukelia išmetamosios dujos, kietosios dalelės, kurias į atmosferą išskiria automobiliai, pramonė. Siekiant mažinti klimato kaitą, gyventojai turėtų atsakingai vartoti, keliauti. Pasaulyje plinta įvairios prieš klimato kaitą kovojančios iniciatyvos, pavyzdžiui, skrydžio gėdos judėjimas.

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Yra ir reikšmingų darbų su **lietuviškomis pavardėmis**. Pvz.,

## **Darius Ceburnis**

**Natl Univ Ireland Galway, Sch Phys, Univ Rd, Galway, Ireland**

**Per 140 str., cituotas per 7000 kartų**

### **Keletas darbų:**

O'Dowd, C., Facchini, M., Cavalli, F. .. **Darius Ceburnis** (Airija), et al. Biogenically driven organic contribution to marine aerosol. **Nature** **431**, 676 (**2004**).

... **Darius Ceburnis**, et al. ...aerosol particle formation ... **Nature** **537**, 532 (**2016**).

...**Darius Ceburnis**, et al. ....cloud droplet... **Nature** **546**, 637 (**2017**).

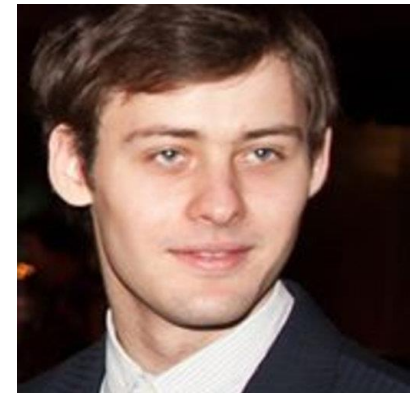
Ch. Lin, **D. Ceburnis** et al, Air quality—climate forcing double whammy from domestic firelighters, **npj Climate Atmosph. Sc.** **6**, 101 (**2023**)





## Vėlesni mūsų grupės artimos tematikos darbai

- ✓ J. Ruseckas, R. Kazakevičius and B. Kaulakys,  $1/f$  noise from point process and **time-subordinated Langevin equations**. J. Stat. Mech. **2016**, P054022 (2016).
- ✓ J. Ruseckas, R. Kazakevičius and B. Kaulakys, **Coupled nonlinear stochastic differential equations** generating arbitrary distributed observable with  $1/f$  noise, J. Stat. Mech. **2016**, P043209 (2016).
- ✓ R. Kazakevičius, A. Kononovicius, B. Kaulakys, V. Gontis. Understanding the nature of **the long-range memory phenomenon in socio-economic systems**. Entropy **23**: 1125 (2021).
- ✓ A. Kononovicius, B. Kaulakys.  **$1/f$  noise from the sequence of nonoverlapping rectangular pulses**. Physical Review E **107**: 034117 (2023).
- ✓ R. Kazakevičius, A. Kononovicius, **Anomalous diffusion** and **long-range memory** in the **scaled voter model**, Phys. Rev. E **107**, 024106 (2023)
- ✓ A. Kononovicius, B. Kaulakys.  **$1/f$  noise in electrical conductors** arising from the heterogeneous detrapping process of individual charge carriers. (to be published)



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## Giorgio Parisi tyrimai sunkiai aprèpiami

Around 1980, **Giorgio Parisi discovered hidden patterns** in disordered complex materials.

His discoveries are **among the most important contributions to the theory of complex systems.**

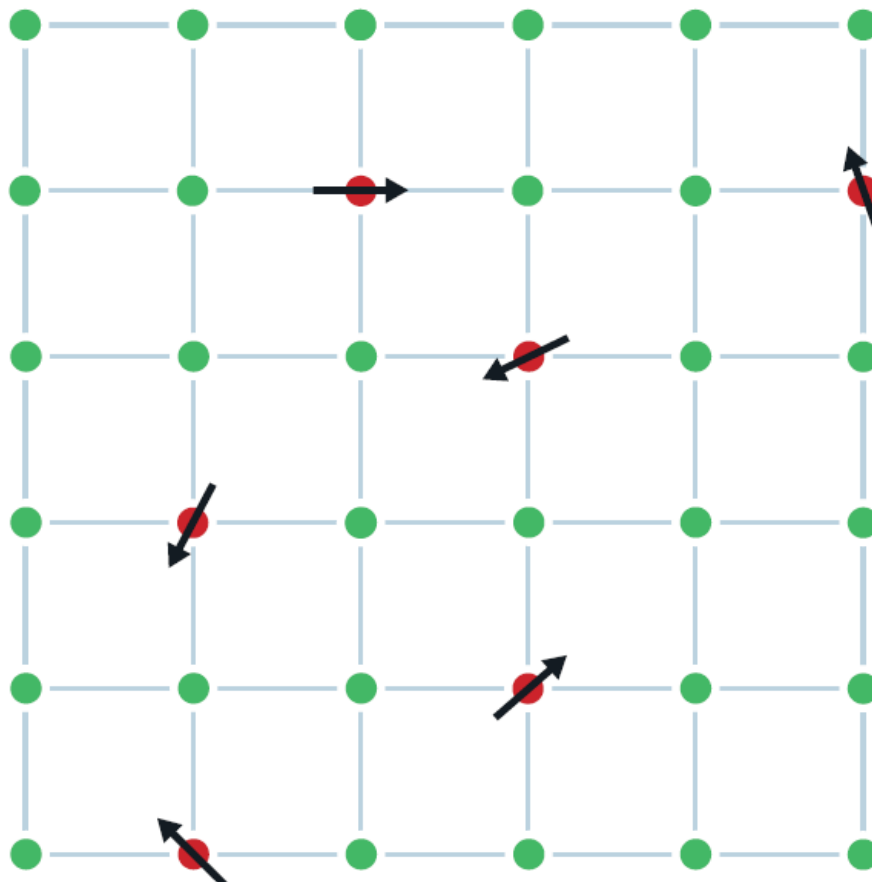
They make it possible to understand and describe many different and apparently entirely **random complex materials and phenomena,**

not only in **physics**

but **also in other, very different areas,**

such as **mathematics, biology, neuroscience and machine learning....**

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● Iron  
● Copper

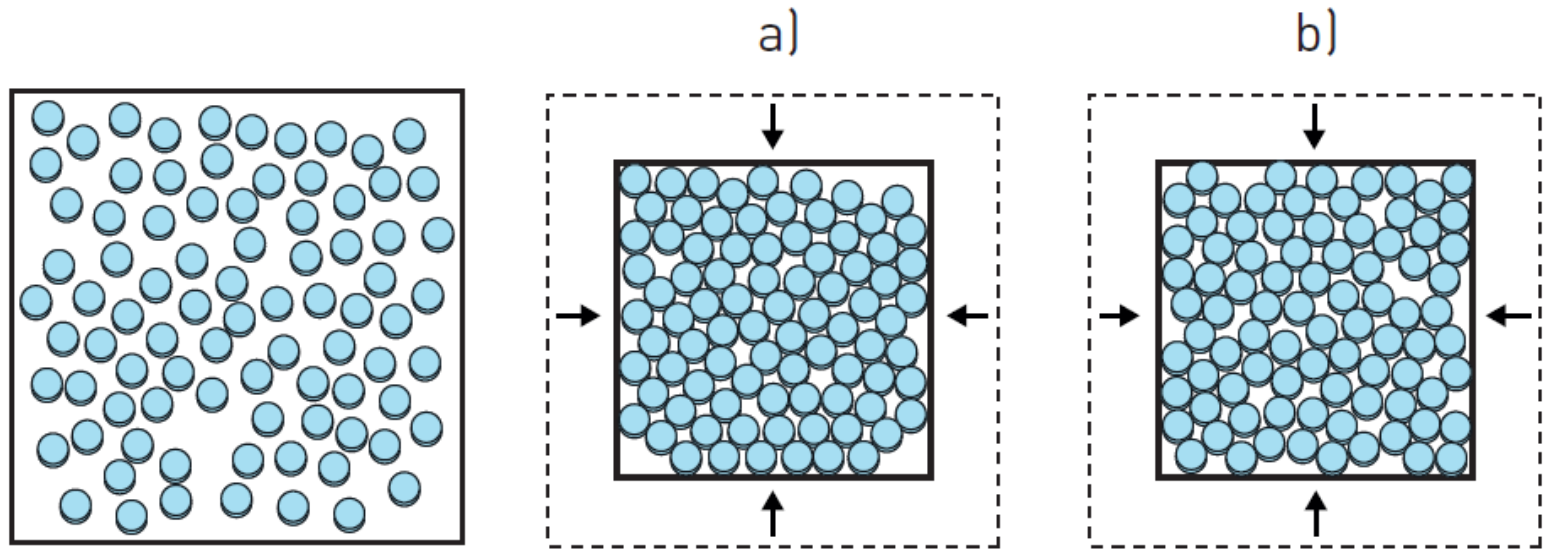
## Sukininiai stiklai

A **spin glass** is a metal alloy where iron atoms, for example, are randomly mixed into a grid of copper atoms.

**Each iron atom behaves like a small magnet, or spin**, which is affected by the other magnets around it.

However, in a spin glass they are frustrated and have difficulty choosing which direction to point.

Using his studies of spin glass, **Parisi developed a theory of disordered and random phenomena that covers many other complex systems.**



## Mathematics for complex disordered systems

Every time many identical discs are squeezed together, **a new irregular pattern is formed despite them being squeezed in exactly the same way.**

What governs the result?

**Giorgio Parisi discovered a hidden structure in such complex disordered systems, which these discs represent, and found a way of describing them mathematically.**

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## **Giorgio Parisi solved the problem of replica symmetry breaking**

by realizing that, in contrast to ferromagnets which have only two "pure states" (up/down) in the ordered phase, **there must be an infinite number within the ordered phase of the spin glass.**

Not only did this provide the solution, but it had a stunning array of **extensions to a wide range of spin-glass and other systems**

**G. Parisi, Infinite number of order parameters for spin-glasses** Phys. Rev. Lett. 43, 1754 (1979).

**G. Parisi, Statistical Field Theory** (Addison-Wesley, Redwood City, CA, 1988, pp. 352)

The broad reach of broken replica symmetry concepts and methods has exploded since Parisi's original work. In particular,

Parisi and his collaborators have shown that in John Hopfield's **neural network model**, and its many offspring, the multiple memories stored in the network correspond to the **multiple equilibria of the spin glass.**

Moreover, their methods allowed them to address the **classical optimization problem of the traveling salesman who stops at many local minima but of course the global minimum/minima are the targets of interest.**

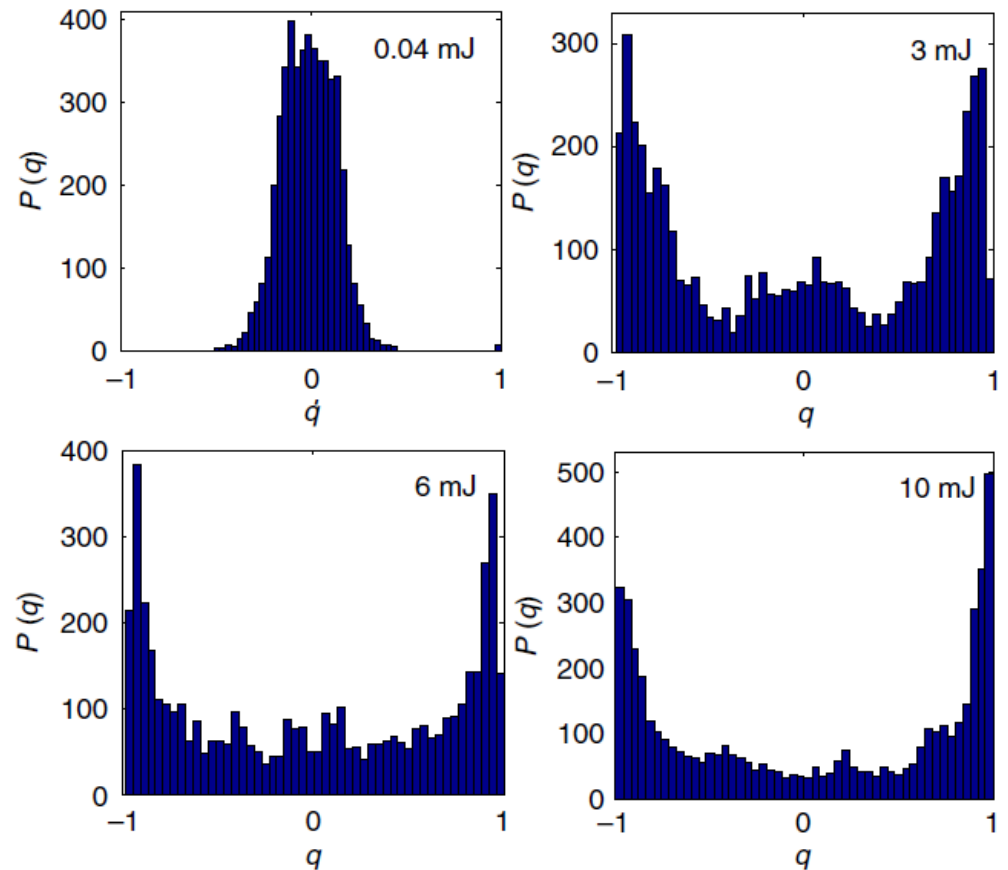
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## Random laser

The theoretical interest in random lasers in connection with replica

**symmetry breaking...**

In random lasers it is possible to observe directly **the occupancy of different harmonic modes** and therefore one can measure directly the function  $P(q)$ .



The distribution  $P(q)$  of the overlap  $q$  for **different pump energies**.

**The pump energy plays the role of the inverse temperature.**

As the pump energy increases the distribution of first order replica **symmetry breaking appears.**

R. Benzi, G. Paladin, **G. Parisi**, A. Vulpiani, On the **multifractal nature of fully developed turbulence and chaotic systems**, J. Phys. A **17** 3521 (1984).

M. Mezard, **G. Parisi**, R. Zecchina, Analytic and Algorithmic Solution of Random Satisfiability Problems. **Science** **297**, 812 (2002).

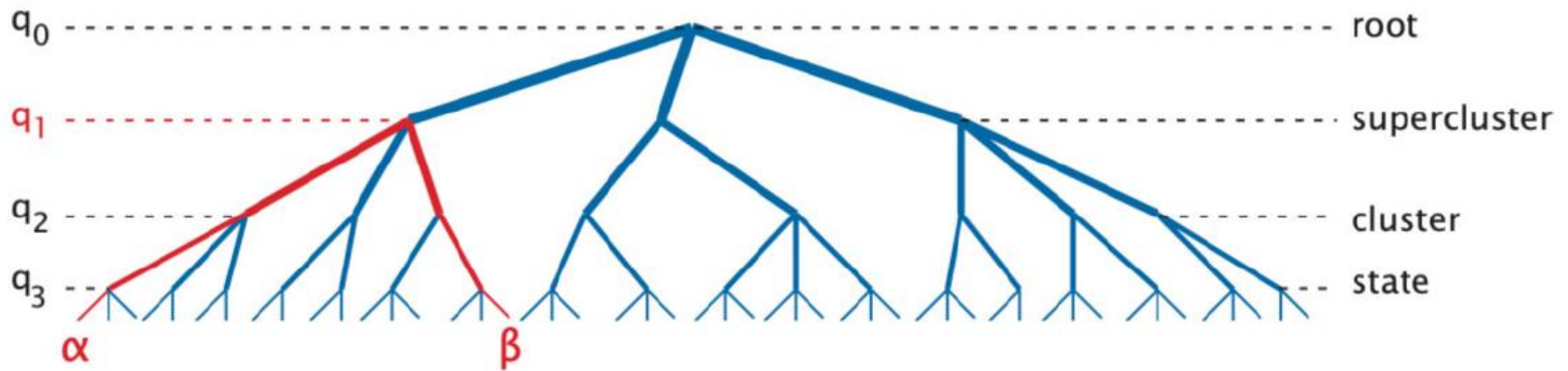
**G. Parisi** and F. Zamponi, Mean-field theory of hard sphere glasses and jamming. **Rev. Mod. Phys.** **82**, 789 (2010).

**G. Parisi**, **Physics, complexity and biology**. Advan. Compl. Syst. **10**, 223 (2007).

J-P Bouchaud, M. Mézard, and **G. Parisi**. Scaling and **intermittency** in **burgers** turbulence. Phys. Rev. E, 52(4):3656, 1995.

P. Rissone, E.I. Corwin, **G. Parisi**, Long-Range Anomalous Decay of the **Correlation** in Jammed Packings. **Phys. Rev. Lett.** 127, 038001 (2021).

**G. Parisi**, **Nobel Lecture: Multiple equilibria**, **Rev. Mod. Phys.** **95**, 030501 (2023).





## Italijos mokslininkai ragina žiniasklaidą geriau paaikškinti klimato kaitą

Laišką, atsiųstą iš Italijos Klimato žiniasklaidos centro, pasirašė ir **2021 m. Nobelio fizikos premijos laureatas Giorgio Parisi** iš Romos Sapienzos universiteto.

„Karščio bangos, potvyniai, užsitęsusios sausros ir gaisrai yra tik keletas požymių, rodančių, kad klimato kaitos poveikis mūsų teritorijoms stiprėja“, – sakoma 96 mokslininkų pasirašytame laiške

„Tačiau **Italijos žiniasklaida vis dar per dažnai kalba apie „blogą orą“, o ne apie klimato kaitą.**

**Kalbėdama apie tai, ji dažnai nutyli priežastis ir sprendimus**“,

....**karščio bangos tapo labiau tikėtinos dėl klimato kaitos.**  
...pasaulio temperatūra kyla, prognozuojama, kad karščio bangos taps dažnesnės ir intensyvesnės, o jų poveikis bus didesnis.

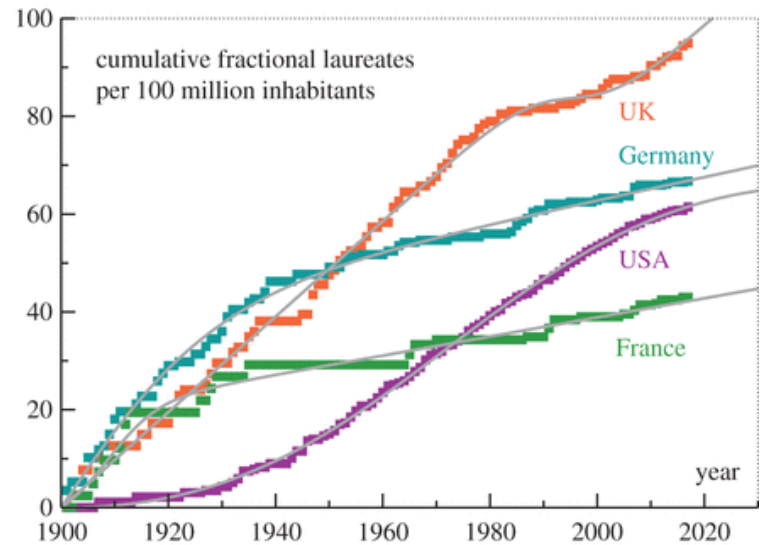
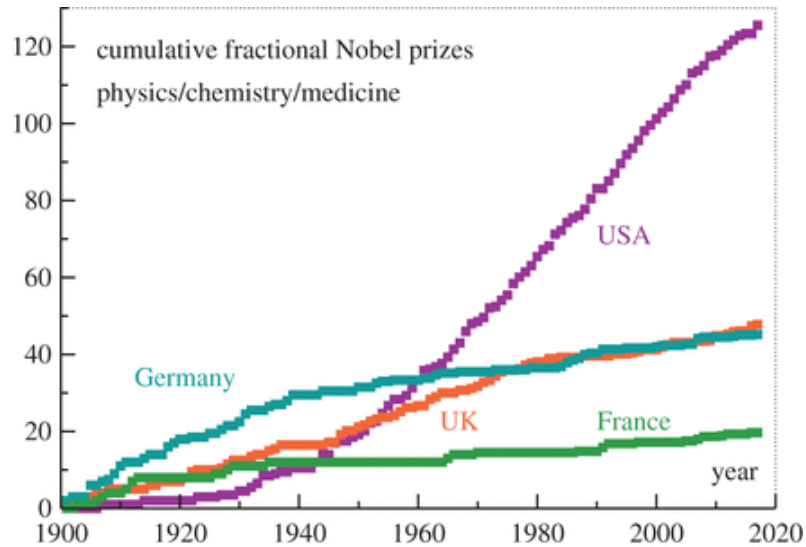
...**dėl pasikeitusių kritulių kylanti temperatūra ir padidėjęs sausumas sukuria idealias sąlygas krūmynų ar miškų gaisrams.**



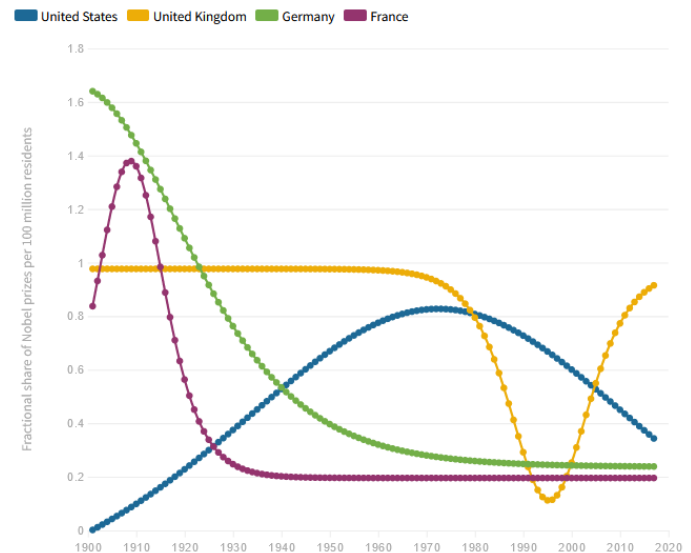
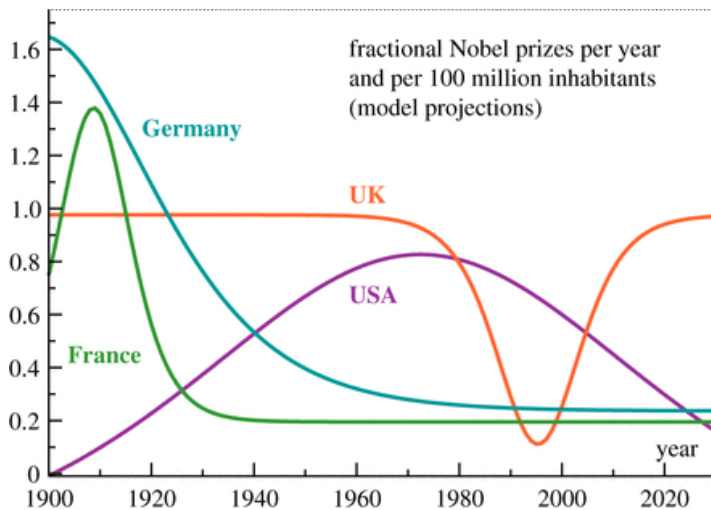
**VU klimatologas Justinas Kilpys:**

... **“įžengėme į teritoriją, kurios nebuvo per pastaruosius milijoną metų” ...**

# Šiek tiek Nobelio premijų statistikos



## Bando aprašyti formulėmis



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**Ačiū už dėmesį !**

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